## iTech Labs

## Blackjack Card Analysis - July 2019

## The Directors

GVC Plc

This is to confirm that iTech Labs has examined the game logs for blackjack games for the period July 01, 2019 to July 31, 2019 as recorded by the respective game servers. The game logs were for blackjack games using 8 decks. iTech Labs has analysed the blackjack cards for statistical randomness. The results of the analysis are given below.

URLs: https://www.bwin.be/, https://www.bwin.dk/, https://www.bwin.es/, https://www.bwin.it/, https://www.bwin.gr/, https://www.bwin.se/, https://www.bwin.com/, https://en.casinoclub.com/, https://bingo.cheekybingo.com/en/bingo, https://da.partypoker.com/, https://danskespil.dk/. https://www.foxybingo.com/, https://casino.foxycasino.com/en/casino, https://sports.gamebookers.com/en/sports, https://www.giocodigitale.it/, https://www.br.betboo.com/en, https://www.partypremium.com, https://www.partypoker.es/en, https://www.partypoker.com/, https://sports.premium.com/en/sports, https://poker.partypoker.se/sv/poker, https://sports.sportingbet.com/en/sports, https://sports.sportingbet.gr/el/sports, https://www.sh.bwin.de/, https://sports.vistabet.com/el/sports, https://sports.sportingbet.co.za/en/sports

## 1. Actual and Theoretical probabilities for Blackjack, 20 and 10

The following tables compare the observed proportion of times the various types of events occurred (Sample column) to the theoretical values (Probability column). Lower and Upper are the 95\% confidence limits.

## Actual and Theoretical probabilities (8 decks)

| Description | Probability | Lower | Sample | Upper |
| :--- | :---: | :---: | :---: | :---: |
| Dealer Blackjack | 0.047451 | 0.04408 | 0.04763 | 0.05083 |
| Player Blackjack | 0.047451 | 0.04468 | 0.04838 | 0.05023 |
| Dealer total 20 (from first 2 cards) | 0.106024 | 0.10114 | 0.10384 | 0.11091 |
| Player total 20 (from first 2 cards) | 0.106024 | 0.10201 | 0.10541 | 0.11004 |
| Dealer hole card is 10 value card (10-J-Q-K) | 0.307692 | 0.30037 | 0.30550 | 0.31502 |

Result: All sample values are within the $95 \%$ confidence limits.

## 2. Actual and theoretical probabilities for Ranks

The following tables compare theoretical probabilities against actual probabilities for the ranks of all cards dealt. Theoretical probabilities are shown in the Probability column. The Sample column shows observed probabilities for all cards dealt to Player and Dealer. Lower and Upper are the 95\% confidence limits.

## Actual and Theoretical probabilities (8 decks)

| Rank | Probability | Lower | Sample | Upper |
| :--- | :---: | :---: | :---: | :---: |
| $\mathbf{A}$ | 0.076923 | 0.07516 | 0.07664 | 0.07868 |
| $\mathbf{2}$ | 0.076923 | 0.07516 | 0.07722 | 0.07868 |
| $\mathbf{3}$ | 0.076923 | 0.07516 | 0.07583 | 0.07868 |
| $\mathbf{4}$ | 0.076923 | 0.07516 | 0.07644 | 0.07868 |
| $\mathbf{5}$ | 0.076923 | 0.07516 | 0.07696 | 0.07868 |
| $\mathbf{6}$ | 0.076923 | 0.07516 | 0.07620 | 0.07868 |
| $\mathbf{7}$ | 0.076923 | 0.07516 | 0.07697 | 0.07868 |
| $\mathbf{8}$ | 0.076923 | 0.07516 | 0.07784 | 0.07868 |
| $\mathbf{9}$ | 0.076923 | 0.07516 | 0.07762 | 0.07868 |
| $\mathbf{1 0}$ | 0.076923 | 0.07516 | 0.07702 | 0.07868 |
| $\mathbf{J}$ | 0.076923 | 0.07516 | 0.07666 | 0.07868 |
| $\mathbf{Q}$ | 0.076923 | 0.07516 | 0.07786 | 0.07868 |
| $\mathbf{K}$ | 0.076923 | 0.07516 | 0.07674 | 0.07868 |

Result: All sample values are within the $95 \%$ confidence limits.

## 3. Comparison of Player's and Dealers first two cards

Using production data, we have calculated the distribution of the first two cards dealt to the player and the dealer. The following table compares the observed proportion of times the player and the dealer have received the cards shown in the Sample column. Lower and Upper are the 95\% confidence limits.

## Comparison of Player's and Dealers first two cards (8 decks)

| Cards | Probability | Lower | Player <br> (Sample) | Upper | Lower | Dealer <br> (Sample) | Upper |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :--- |
| Ace | 0.07692 | 0.07446 | 0.07723 | 0.07938 | 0.07393 | 0.07518 | 0.07991 |
| $\mathbf{2}$ | 0.07692 | 0.07446 | 0.07645 | 0.07938 | 0.07393 | 0.07833 | 0.07991 |
| $\mathbf{3}$ | 0.07692 | 0.07446 | 0.07559 | 0.07938 | 0.07393 | 0.07613 | 0.07991 |
| $\mathbf{4}$ | 0.07692 | 0.07446 | 0.07583 | 0.07938 | 0.07393 | 0.07810 | 0.07991 |
| $\mathbf{5}$ | 0.07692 | 0.07446 | 0.07741 | 0.07938 | 0.07393 | 0.07669 | 0.07991 |
| $\mathbf{6}$ | 0.07692 | 0.07446 | 0.07552 | 0.07938 | 0.07393 | 0.07839 | 0.07991 |
| $\mathbf{7}$ | 0.07692 | 0.07446 | 0.07648 | 0.07938 | 0.07393 | 0.07731 | 0.07991 |
| $\mathbf{8}$ | 0.07692 | 0.07446 | 0.07832 | 0.07938 | 0.07393 | 0.07567 | 0.07991 |
| $\mathbf{9}$ | 0.07692 | 0.07446 | 0.07825 | 0.07938 | 0.07393 | 0.07787 | 0.07991 |
| $\mathbf{1 0}$ | 0.07692 | 0.07446 | 0.07738 | 0.07938 | 0.07393 | 0.07593 | 0.07991 |
| $\mathbf{J}$ | 0.07692 | 0.07446 | 0.07623 | 0.07938 | 0.07393 | 0.07760 | 0.07991 |
| $\mathbf{Q}$ | 0.07692 | 0.07446 | 0.07707 | 0.07938 | 0.07393 | 0.07724 | 0.07991 |
| $\mathbf{K}$ | 0.07692 | 0.07446 | 0.07823 | 0.07938 | 0.07393 | 0.07557 | 0.07991 |

Result: All sample values are within the $95 \%$ confidence limits.

## 4. Comparison of Player's opening score against the dealers opening score

Player's opening scores (2-20) is compared against Dealer's opening scores (2-20). Opening scores are calculated from the first 2 cards for the Player and the Dealer. Probability column shows theoretical probabilities for Player and Dealer. Sample columns show actual values for Player and Dealer. Lower and Upper are the $95 \%$ confidence limits. To simplify the analysis, Ace is counted as 1 .

## Comparison of Player's \& Dealer's opening scores (8 decks)

| Opening <br> score | Probability | Lower | Player <br> (Sample) | Upper | Lower | Dealer <br> (Sample) | Upper |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 0.00575 | 0.0048 | 0.0057 | 0.0067 | 0.0045 | 0.0042 | 0.0069 |
| 3 | 0.01186 | 0.0105 | 0.0107 | 0.0133 | 0.0101 | 0.0121 | 0.0136 |
| 4 | 0.01761 | 0.0159 | 0.0170 | 0.0193 | 0.0155 | 0.0173 | 0.0197 |
| 5 | 0.02373 | 0.0217 | 0.0242 | 0.0257 | 0.0213 | 0.0234 | 0.0261 |
| 6 | 0.02947 | 0.0273 | 0.0289 | 0.0317 | 0.0268 | 0.0283 | 0.0322 |
| 7 | 0.03559 | 0.0332 | 0.0368 | 0.0380 | 0.0326 | 0.0374 | 0.0385 |
| 8 | 0.04133 | 0.0387 | 0.0409 | 0.0439 | 0.0382 | 0.0420 | 0.0445 |
| 9 | 0.04745 | 0.0447 | 0.0484 | 0.0502 | 0.0441 | 0.0461 | 0.0508 |
| 10 | 0.05320 | 0.0503 | 0.0518 | 0.0561 | 0.0496 | 0.0531 | 0.0568 |
| 11 | 0.09490 | 0.0911 | 0.0952 | 0.0987 | 0.0903 | 0.0965 | 0.0996 |
| 12 | 0.08879 | 0.0851 | 0.0891 | 0.0925 | 0.0843 | 0.0866 | 0.0933 |
| 13 | 0.08304 | 0.0794 | 0.0798 | 0.0866 | 0.0787 | 0.0861 | 0.0874 |
| 14 | 0.07692 | 0.0734 | 0.0747 | 0.0804 | 0.0727 | 0.0797 | 0.0812 |
| 15 | 0.07118 | 0.0678 | 0.0722 | 0.0745 | 0.0671 | 0.0727 | 0.0753 |
| 16 | 0.06506 | 0.0618 | 0.0673 | 0.0683 | 0.0611 | 0.0638 | 0.0690 |
| 17 | 0.05931 | 0.0562 | 0.0596 | 0.0624 | 0.0556 | 0.0602 | 0.0631 |
| 18 | 0.05320 | 0.0503 | 0.0552 | 0.0561 | 0.0496 | 0.0525 | 0.0568 |
| 19 | 0.04745 | 0.0447 | 0.0489 | 0.0502 | 0.0441 | 0.0458 | 0.0508 |
| 20 | 0.09416 | 0.0904 | 0.0935 | 0.0980 | 0.0895 | 0.0922 | 0.0988 |

Result: All sample values except one (1) are within the $95 \%$ confidence limits.

## Comments for 8 decks Blackjack

In the calculations for "Actual and theoretical probabilities for Blackjack, 20, 10", "Ranks for all cards", "Ranks for the first 2 cards" and "Comparison of Player's opening score against the dealers opening score", 1 out of 82 sample values (1.22\%) lie outside the $95 \%$ confidence limits. It is acceptable for about $5 \%$ of the confidence limits to be exceeded.

## 5. Conclusion

Calculations for "Actual and theoretical probabilities for Blackjack, 20, 10", "Ranks for all cards", "Ranks for the first 2 cards" and "Comparison of Player's opening score against the dealers opening score" indicated statistical randomness. The results were satisfactory for 8 deck blackjack. iTech Labs concludes that the Random Number Generator is operating correctly and the random numbers are being used in a fair manner.

There were a large enough number of game records to give the probability calculations sufficient statistical power. iTech Labs has done limited sanity checks to verify the integrity of the game logs. iTech Labs also maintains a copy of the game logs for verification purposes.
The scope of the review did not include reviews of financial controls or casino operations. We believe that the probabilities were calculated correctly from the game logs.

Please click here to see the Original report.

## Signed:

## Signed:



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Date: 19 August 2019


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Disclaimer.
While it is not possible to test all possible scenarios in a laboratory environment, iTech Labs has conducted a level of testing appropriate for a component test of this type.


